

1) Find the values of constants  $A$  and  $B$  so that  $\frac{6}{3n+4} = \frac{A}{3n+4} + \frac{B}{3n-1}$ .

2) Find the domain for each of the following functions. State your answers in interval notation.

a.  $y = \sqrt{\frac{x^2 + x - 2}{x^2 - x - 20}}$       b.  $y = \log x^3 - 3x^2$

3) Simplify. Show your reasoning.

a.  $\tan \theta \cdot \cot \theta - \cos^2 \theta$       b.  $\csc x - \cot x - \frac{\sin x}{1 + \cos x}$

4) Solve the equation for  $x$  in the indicated domain:

$$4\sin^2(x) + 6\csc^2(x) = 11, \quad 0 \leq x < 2\pi$$

5) Let  $a_n = \left(\frac{1}{2}i\right)^n$ , where  $i = \sqrt{-1}$ , the imaginary unit. You will want to use your calculator for this question.

a) State the first 8 terms of  $a_n$  exactly.

b) State the first 6 terms of  $S_n$  where  $S_n = \sum_{i=1}^n a_n$ .

c) Using the  $\sum$  key on your calculator, give a twelve decimal approximation for  $\sum_{k=1}^{20} \left(\frac{1}{2}i\right)^k$ ,

$$\sum_{k=1}^{200} \left(\frac{1}{2}i\right)^k, \text{ and } \sum_{k=1}^{1000} \left(\frac{1}{2}i\right)^k.$$

6) In  $\triangle ABC$ ,  $b = \sqrt{5}$ ,  $c = \sqrt{17}$  and  $\cos B = \frac{4}{\sqrt{17}}$ . Find the exact value of  $a$ .

7) Let  $f(x) = 3x^2 + 2x - 5$ . Simplify:  $\frac{f(x+h) - f(x-h)}{2h}$ .

8) Find all values of  $x$  for which the geometric series  $S = 1 + 2(x-3) + 4(x-3)^2 + 8(x-3)^3 + \dots$  converges. Then, assuming these values for  $x$ , find  $S$  in terms of  $x$  as a simple fraction.

9) Find the sum of all multiples of 12 between 100 and 1000.

10) State the expanded form of  $\sum_{i=0}^n \binom{n}{i}$  and give its sum. You will want to use ‘. . .’ in your expansion.

11) On his daughter’s first birthday, Dr. Condie deposits \$ 1,000 into an account that pays 6.8% compounded annually. Each succeeding birthday he deposits another \$ 1,000.

- Using  $\sum$  notation, write an expression for the amount in the account on her 18<sup>th</sup> birthday after his deposit.
- Determine the total amount in the account on that day.
- How much must he deposit each year for the account to be worth \$ 100,000 by her 18<sup>th</sup> birthday?

12) Find, to the nearest hundredth of a degree, the angle formed by the two “main” diagonals of a cube.

13) Consider the sequence: 
$$\begin{cases} a_1 = 1 \\ a_2 = 1 \\ a_n = 5a_{n-2} + 2a_{n-1} \end{cases}$$

- State the first 8 terms of the sequence.
- Let  $G_n = \frac{a_{n+1}}{a_n}$ . Find  $G_5$ .
- Give a five decimal approximation of  $\lim_{n \rightarrow \infty} G_n$ .

14) Evaluate the following extended fraction: 
$$2 + \frac{5}{2 + \frac{5}{2 + \frac{5}{2 + \frac{5}{\dots}}}}$$

State your answer exactly and as a five decimal approximation.

15) Consider the sequence: 
$$\begin{cases} a_1 = 5 \\ a_2 = 3 \\ a_n = 5a_{n-2} + 2a_{n-1} \end{cases}$$

- State the first 8 terms of the sequence.
- Let  $G_n = \frac{a_{n+1}}{a_n}$ . Find  $G_5$ . State your answer to five decimal places.
- Give a five decimal approximation of  $\lim_{n \rightarrow \infty} G_n$ .
- State the exact value of  $\lim_{n \rightarrow \infty} G_n$ .

16) Consider the sequence: 
$$\begin{cases} a_1 = 4 \\ a_2 = 6 \\ a_n = 3a_{n-2} + 7a_{n-1} \end{cases}$$

a) Let  $G_n = \frac{a_{n+1}}{a_n}$ . State an extended fraction that equals the exact value of  $\lim_{n \rightarrow \infty} G_n$ .

b) Find the exact value of  $\lim_{n \rightarrow \infty} G_n$ .

17) Write the first 10 terms as reduced fractions of the sequence given by:

$$1, 1+1, 1+\frac{1}{1+1}, 1+\frac{1}{1+\frac{1}{1+1}}, 1+\frac{1}{1+\frac{1}{1+\frac{1}{1+1}}}, \dots$$

18) A Ferris wheel with a diameter of 20 m rotates at a rate of 2 minutes per revolution. Riders board the Ferris wheel 1 m above the ground at the bottom of the wheel. A couple boards the Ferris wheel and the ride starts.

- How far above the ground is the couple 40 seconds after the ride starts?
- How many seconds will it be (after the ride starts) before the couple is 10 m above the ground for the *second time*?